

# DAY -TO- DAY - VARIABILITY IN SOME IONOSPHERIC PARAMETERS IN THE QUIET EQUATORIAL IONOSPHERE (CASE STUDY: f<sub>o</sub>F<sub>2</sub>)

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## Abstract

The F<sub>2</sub> region of the Ionosphere is a complex one. There are large irregular changes of foF<sub>2</sub> from day - to - day. This paper discusses the diurnal and seasonal variations of f<sub>o</sub>F<sub>2</sub>. While the diurnal variation of foF<sub>2</sub> has a maximum value at a time far from mid-day, the seasonal variation curve has two maximum points in the months of March and November respectively, with a minimum in July. Thus, indicating that the seasonal variation of foF<sub>2</sub> is a semi - annual one. It was also shown that for short time variations, the day-to-day variability in f<sub>o</sub>F<sub>2</sub> is neither due to season nor relative sunspot number, Rz. The test of significance between the standard errors of foF<sub>2</sub> before and after correction for season and Rz show no significant difference at 95% level of significance.

The Ionosphere consists of a number of ionized regions above the earth's surface at a height of 60km to 100km containing ions which play an important role in the propagation of radio waves. It is made up of three layers namely; the D, E and F regions. The region in which this study is based is the F region- ionized region above E region which is further divided into fi and F2 layer in day- time. It is the critical frequency of Fj region that is used for this study.

The predominant ions are No<sup>+</sup> and O<sup>+</sup>2 in the F region produced by electromagnetic radiation. In particular, the phenomenology of F2 region is very complex in that the F2 region is very thick with electron density of about 10<sup>6</sup>/cm<sup>3</sup>. The F2 region is highly anomalous. Some of these anomalies include geographic, diurnal, seasonal and eclipse.

The diurnal variation of foFa has been observed to vary from time to time and occur with a valley near noon, often called the neon bite out effect. It has also been remarked that there is a well marked semi-annual variation in both maximum electron density and the total columnar ionization of the F2 layer and hence foF<sub>2</sub> of the F2 region (Bates, 1960). There is the world wide result summarized by (Retcliffe, 1960) in the expression  
(f<sub>o</sub>F<sub>2</sub>)<sub>a</sub> (1 + 0.02Rz)

Where Rz is the mean Zurich sunspot number. This shows that ft»F2 varies with sunspot number, hence establishing a kind of solar cycle variation (variation of 1 1 year periodicity) The purpose of this study therefore is to investigate all the above using Ibadan data,

## Data Collection

The data used in this study were collected from the readings of an Ionosonde, which were recorded, into booklets. The Ionosonde is the ionospheric sounder used in Ibadan . Ibadan has geographical coordinates 07° 24<sup>7</sup>N, 03°54<sup>4</sup>. The period covered by data is January to December 1998. it was a year of sunspot maximum and when ionospheric recordings were adequately made.

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**Criteria Used For Quiet Day and Terminologies Used.**

The selection of quiet days was based on data readily available and the Ap indices (geomagnetic amplitudes) which are more influenced by short term transient variations for which a satisfactory estimate of Ap less than or equal to 10 ( $A_p < 10$ ) was taken as indicating a magnetically quiet day (arbitrary) and the results, therefore describe the behaviour of the undisturbed F region.

**Terminologies Used**

Time: Time refers to as local mean time.

Daytime: Hours between 0600 and ISOOhrs.

Nighttime: Hours between 1900 and OSOOhrs.

Seasons: Following the division of the year into seasons by Danilov, and Mikhailov (2004), the different seasons are given by March and April representing March equinox, September and October representing September equinox, May to August representing June solstice, and November to February representing December solstice,

foFa is the ordinary wave critical frequency of the F2 layer.

**Analysis**

**Diurnal Variation**

The observed values of foF2 at each hour of the day, representing September equinox, June solstice and December solstice are shown in tables 1(A and B),2 (A and B)and 3(A and B) respectively.

**September Equinox (Month of September) F<sub>o</sub>f<sub>2</sub> Values (Observed) MHZ**

00	01	02	03	04	05	06	07	08	09	10	11	12	13
7.3	7.1	8.7	8.4	8.5	7.9	9.3	122	-	148	143	129	125	121
8.1	7.9	8.6	8.7	8.5	8.5	9.0	121	-	148	152	145	133	127
7.8	7.6	7.4	7.6	7.2	5.3	8.5	118	134	128	130	121	119	118
8.6	100	8.6	8.4	7.0	3.7	8.3	119	135	-	145	143	141	136
-	-	-	-	-	-	-	-	140	149	-	139	132	120
-	-	-	-	7.3	6.3	8.3	118	136	148	149	142	132	128
1.1	112	114	108	7.7	6.2	8.5	118	135	140	136	125	129	121
0.8	109	8.5	8.2	6.2	3.6	7.9	112	131	140	146	-	142	143
0.2	100	9.8	7.9	5.8	3.8	8.0	113	127	125	115	115	117	118

**Day -To- Day - Variability in Some Ionospheric Parameters in the Quiet Equatorial Ionosphere (Case Study: F<sub>o</sub>F<sub>2</sub>)**

**Table 1a**

14	15	16	17	18	19	20	21	22	23	Rz
12.0	11.8	11.8	11.6	11.3	8.6	8.7	8.6	8.6	8.6	245

121	11.1	11.1	-	9.4	7.5	6.6	7.2	6.6	7.5	268
122	12.5	12.5	11.7	11.2	9.8	7.5	7.2	7.2	<i>ILL-</i>	265
13.2	12.4	11.7	-	-	-	6.6	-	-	-	233
11.7	11.6	11.3	<i>ILL-</i>	-	8.5	8.4	8.5	10.1	10.7	187
12.6	12.6	12.3	11.6	11.3	9.5	10.4	10.8	10.8	10.9	156
12.2	11.9	11.7	11.5	-	8.6	8.7	8.7	9.0	8.8	172
14.3	14.2	13.8	11.7	11.3	8.3	8.5	8.5	10.5	10.8	175
12.3	12.4	12.5	-	10.3	6.9	8.4	8.3	8.4	8.5	174

**Table Ib**  
**June Solstice (Month of May) F<sub>0</sub>f<sub>2</sub> Values (Observed) Mhz**

00	01	02	03	04	05	06	07	08	09	10	11	12
8.4	8.6	8.6	-	-	-	-	-	137	148	152	147	137
6.6	8.1	8.3	7.9	7.4	5.2	8.5	<i>II</i>	139	151	151	151	142
10.0	9.8	9.5	8.0	3.7	2.7	8.7	105	133	140	129	129	122
0.5	6.4	6.3	6.4	6.1	4.4	8.9	124	137	138	118	<i>IB</i>	115
-	.	-	-	-	5.5	9.2	127	140	141	124	124	120
-	6.4	5.6	5.4	4.7	3.1	-	-	-	-	<i>IV</i>	117	109
4.9	4.8	4.8	5.1	5.2	5.2	9.4	125	138	143	143	143	134
6.7	6.7	6.6	6.3	4.8	3.1	8.5	118	136	140	123	123	<i>IB</i>
6.0	6.0	5.9	5.9	5.1	3.9	8.8	119	137	143	133	133	<i>II</i>

**Table 2a**

13	14	15	16	17	18	19	20	21	22	23	Rz
126	124	122	121	118	104	9.4	7.9	-	-	-	150
134	125	114	109	109	106	-	-	-	-	-	166
120	<i>IV</i>	<i>IV</i>	117	119	109	8.7	-	8.3	7.7	6.6	140
115	<i>IB</i>	<i>IB</i>	115	-	-	-	-	-	-	-	132
115	115	<i>IV</i>	114	115	<i>IB</i>	109	9.2	-	-	-	162
109	109	<i>IV</i>	116	117	-	-	-	-	6.5	5.3	165
127	123	119	120	120	117	9.7	6.6	6.6	6.7	6.7	171
107	106	108	<i>IV</i>	113	111	-	8.6	8.2	-	6.3	204
109	106	109	<i>IV</i>	114	111	108	-	8.3	6.6	6.1	192

**Table 2b**  
**December Solstice (Month of December) foFz Values (Observed) MHz**

00	01	02	03	04	05	06	07	08	09	10	11	12
8.0	8.5	8.9	9.2	8.4	-	.	-	114	<del>10</del>	117	131	-
8.0	9.5	9.1	8.4	7.5	6.7	7.9	10.0	112	<del>10</del>	126	122	124
8.2	8.5	8.3	8.3	8.6	6.7	7.1	9.2	108	108	115	119	115
7.8	8.3	8.2	6.8	6.4	6.6	7.9	-	113	121	128	129	120
3.4	8.4	8.4	8.2	7.1	4.8	6.6	9.4	<del>113</del>	119	134	138	138
8.2	8.3	8.3	7.8	7.2	6.8	7.5	<del>103</del>	115	128	135	132	-
-	-	-	-	-	9.2	-	-	118	119	119	-	105
8.3	8.3	8.4	9.0	8.3	-	-	-	-	-	124	<del>117</del>	<del>112</del>
8.9	8.7	9.6	9.3	8.4	5.5	5.4	9.1	113	-	-	-	-

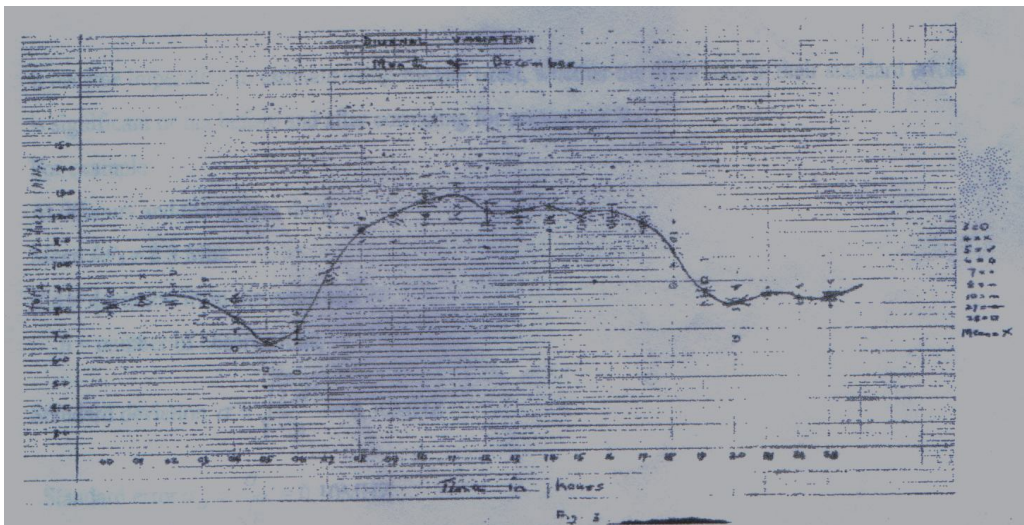
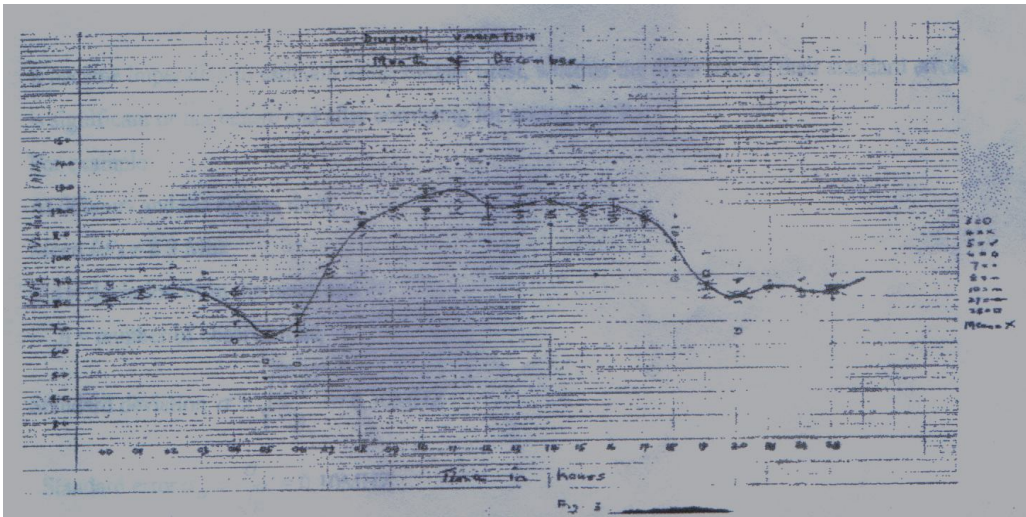
**Table 3a**

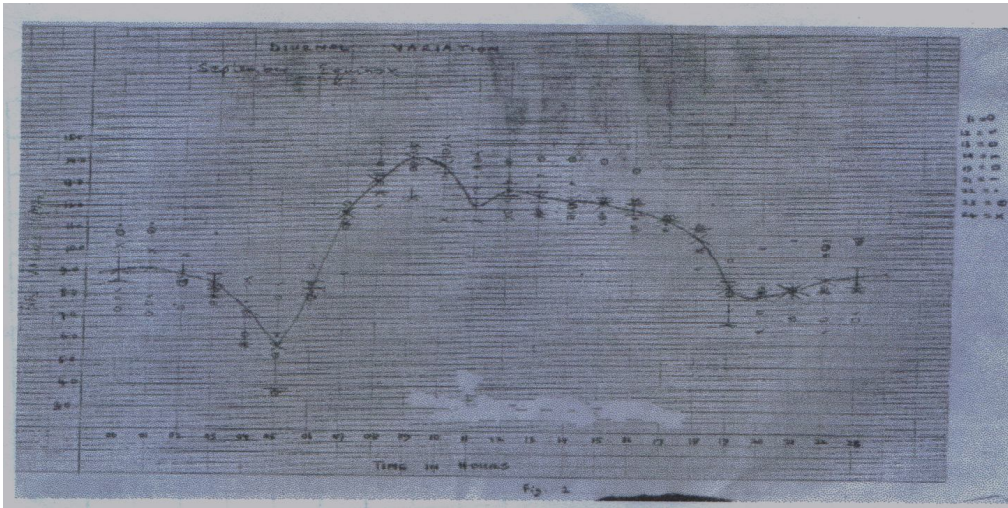
13	14	15	16	17	18	19	20	21	22	23	Rz
117	116	116	<del>114</del>	111	8.8	p	6.6	-	8.1	8.2	200
120	<del>121</del>	116	-	<del>116</del>	9.7	8.6	-	-	-	-	210
115	117	118	<del>117</del>	<del>114</del>	<del>110</del>	8.1	-	-	8.7	8.9	190
120	<del>121</del>	124	-	<del>118</del>	-	-	-	8.3	-	-	192
143	143	-	138	<del>116</del>	<del>116</del>	8.4	8.7	8.7	8.1	7.9	200
128	129	120	117	<del>117</del>	-	8.9	8.8	8.5	8.2	8.3	210
108	112	117	114	<del>118</del>	-	8.6	-	-	8.2	-	250
113	-	-	-	-	-	8.0	-	-	-	-	185
-	115	<del>118</del>	114	<del>114</del>	10.4	9.0	8.2	8.4	8.2	8.4	100

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**Table 3b**

These tables 1,2 and 3 were used to plot the diurnal variation curves for the September equinox, June solstice and December solstice are shown in figs 1,2 and 3 respectively.





It became imperative to estimate using student t-test, whether the difference in their standard errors is significant or not before and after correcting for season and Rz

For example:

At 00hours and the chosen days,

Mean  $f_0F_2=8.3\text{Mhz}$

If  $d$ =deviation from the mean and

$n$ =number of observations,

$$\text{Standard deviation } \sigma = \sqrt{\frac{\sum d^2}{n}} = 0.30\text{MHZ}$$

$$\text{Standard error } \sigma_m = \frac{\sigma}{\sqrt{n}} = 0.10\text{MHZ}$$

Hence  $f_0F_2 = 8.3 \pm 0.10 \text{ MHz}$  (see error bars on graphs)

Similar analysis was carried out at various times of the day on the variation curves.

**Table 4 illustrate the result obtained.**  
**September Equinox**

TIME	00	03	06	10	12	13	16	19	23
A	1.4	0.9	0.4	1.1	0.8	0.8	0.7	0.8	1.3
<V	0.5	0.3	0.1	0.3	0.2	0.2	0.3	0.3	0.4
3a <sub>m</sub>	1.5	0.3	0.3	0.9	0.6	0.6	0.9	0.9	1.2

**June Solstice**

A	1.4	1.0	0.3	0.6	1.1	0.8	0.3	0.7	0.4
Ora	0.5	0.3	0.1	0.2	0.3	0.2	0.1	0.3	0.2
3a <sub>m</sub>	1.5	0.9	0.3	0.6	0.9	0.6	0.3	0.9	~ W

**December Solstice**

<3	0.3	0.7	0.8	0.7	1.0	1.0	0.8	0.3	0.3
O <sub>m</sub>	0.1	0.2	0.3	0.2	0.4	0.3	0.3	0.1	0.1
3a <sub>m</sub>	0.3	0.6	0.9	0.6	1.2	0.9	1.0	0.3	0.3

**Table 4**

**Seasonal Variation**

The mean values of the observed daily values of foF<sub>2</sub>at each hour of the day for each month was computed to study the yearly behaviour of foF<sub>2</sub>. Table 5 below shows the result obtained.

MONTHS	JAN	FEB	MAR	APRIL	MAY	JUNE	JULY	AUGUST	SEPT	OCT	NOV	DEC
foF <sub>2</sub> MHz	12.0	12.5	13.5	13.1	12.4	11.7	11.3	11.7	12.3	12.8	13.0	12.0

**Table 5**



The Table was used to plot the seasonal variation curve shown in fig 4

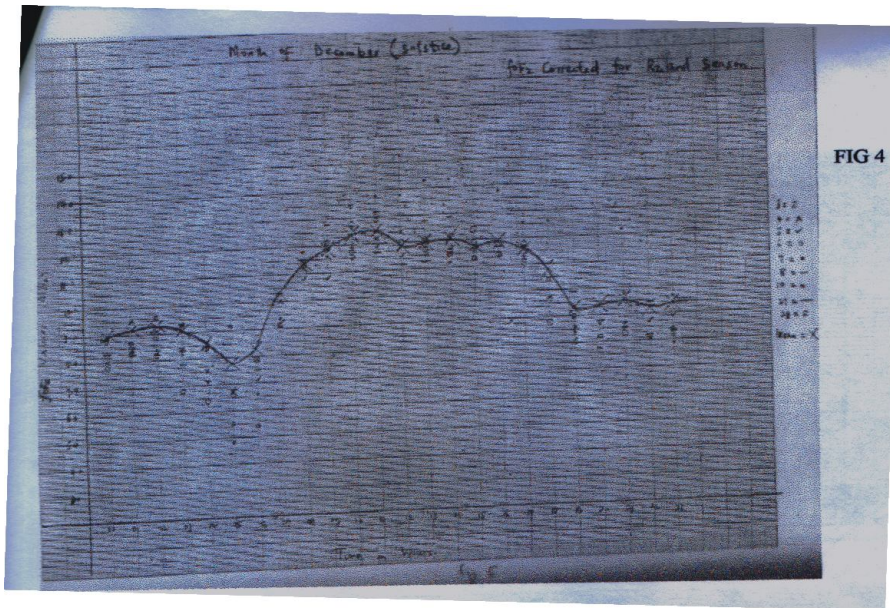
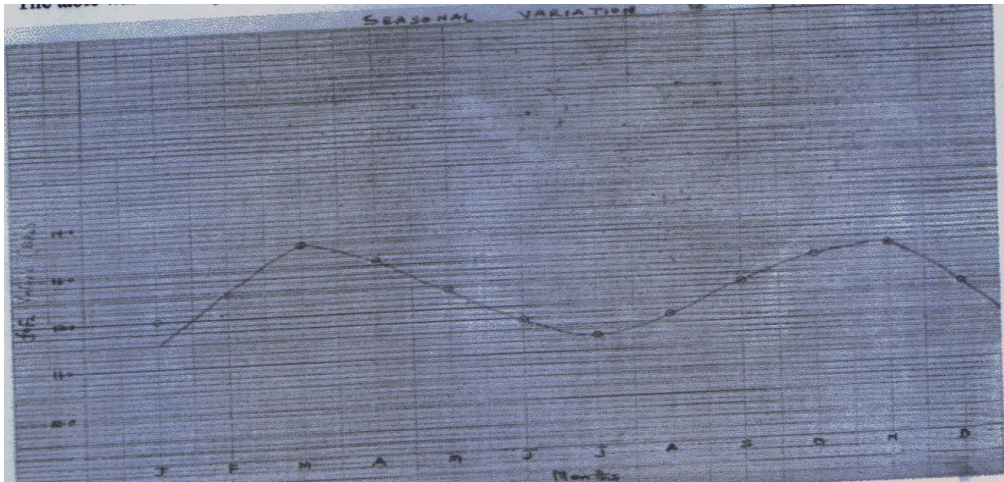
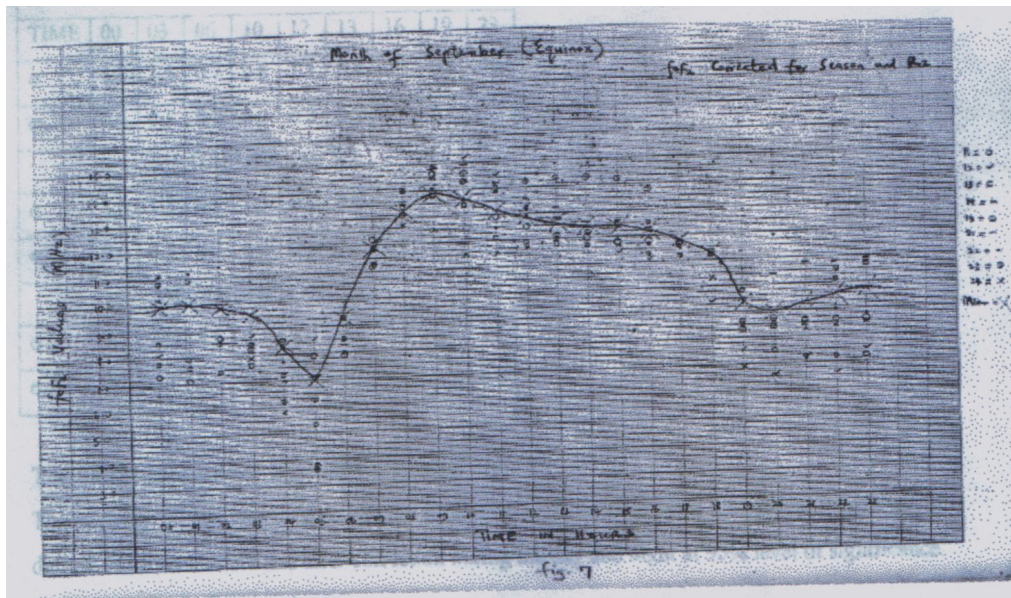
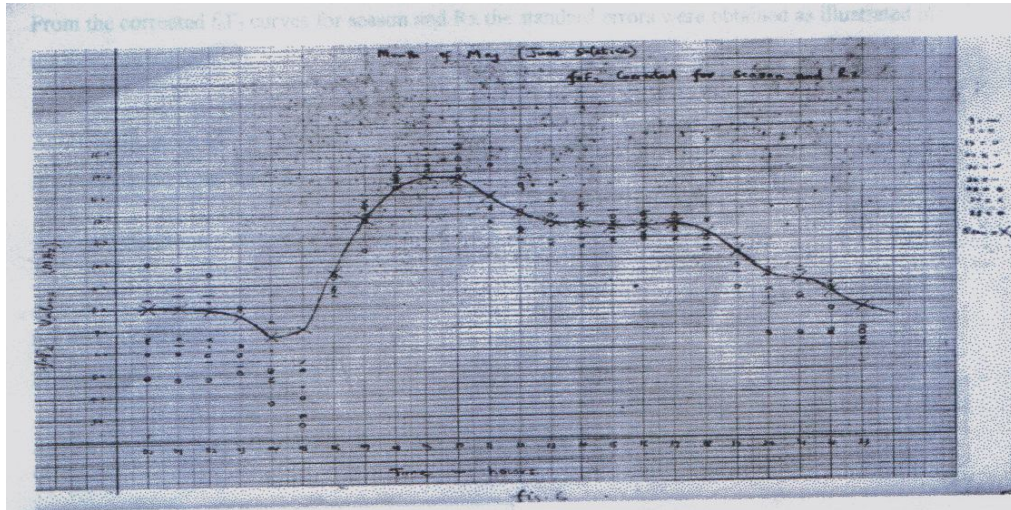


FIG 4



### Corrected f<sub>o</sub>F<sub>2</sub>

It is important to examine the effect of seasonal variation and R<sub>z</sub> on foF<sub>2</sub>. Fig 4 is used to correct for season. (Yokoyama,2004) showed that critical frequency of the F<sub>2</sub> layer is related to the relative sunspot number R<sub>z</sub> by  $f_oF_2 = A + 0.028R_z$ , where A = constant dependent on magnetic dip (Maruyama,1996) using Ibadan data, showed that for short time variations, the constant A is approximately equal to 6.77Mhz (magnetic dip for Ibadan = -6°). The above equation was used to correct for R<sub>z</sub>. The corrected diurnal variation curves are as shown in figs 5,6 and 7 for the solstice and equinox.



From the corrected  $f_0F_2$  curves for season and Rz the standard errors were obtained as illustrated in the example below.

At 00 hours, means  $f_0F_2=8.0$  MHz

If  $d$  = deviation from the mean,

$$\text{Standard deviation} = \sigma = \sqrt{\frac{\sum d^2}{n}}$$

“

$n$  = no of observations.

$$\text{Standard error } \sigma_m = \frac{\sigma}{\sqrt{n}} = 0.7$$

Similar analysis was carried out at various times of the day. Table 6 below shows the results obtained.

<b>September Equinox</b>									
TIME	00	03	06	10	12	13	16	19	23
O	1.8	1.5	0.7	0.8	1.1	0.8	0.3	0.9	0.6
CFm	0.6	0.5	0.2	0.2	0.3	0.2	0.1	0.4	0.7
<b>June Solstice</b>									
O	1.6	1.3	0.9	1.1	0.8	0.8	0.6	1.4	1.5
°m	0.6	0.5	0.3	0.4	0.2	0.2	0.2	0.5	0.5
<b>December Solstice</b>									
O	0.7	1.0	1.5	0.7	1.0	1.0	0.8	0.8	1.1
°m	0.2	0.3	0.6	0.2	0.4	0.3	0.3	0.3	0.4

**Test of Significance For Diurnal Variations**

The students "t" test was used to test the significant difference between the standard errors of the diurnal variations before and after correction during the day and night at 95% level of significance. The results obtained are as shown. 1. Month of May (June Solstice)

Daytime (1000hours)

Before = 0.22

After-0.28

$t=0.11$

**$t_{95\%}=2.31$**

$t_{95\%}>t$  ( **$t=0.11$** )

**Month of September (September Equinox)**

Daytime (1000hours)

**Before-0.38**

After-0.40 t = 0.02

$t_{95\%} - 2.31 > t (t - 0.02)$

**Month of December (December Solstice)**

Daytime (1000hours)

**Before - 0.24**

**After - 0.24**

$t_{95\%} > t (t - 0)$

The above result in each case show no significance at 95% level of significance by day.

**2. Month of May (June Solstice)**

Night time (2300hours)

Before = 0.21

After -0.74 t -0.52

$t_{95\%} - 2.31 > t (t = 0.52)$

**Month of September (September Equinox)**

Night time (2300hours)

Before - 0.49

After = 0.54 t -0.07

$t_{95\%} > t (t - 0.07)$

**Month of December (December Solstice)**

Night time (2300hours)

Before-0.18

After - 0.49 t - 0.46

$t_{95\%} > t (t - 0.46)$

Hence no significant difference between the two standard errors before and after correction for season and Rz at 95% level of significance, by day and by night.

**Summary of Results and Discussion**

From the diurnal variation curves, it is observed that they are large irregular changes of fbF<sub>2</sub> during individual days. The amplitude of variation is greater in daytime than at night.

Essentially, foF<sub>2</sub> at midday (1200hrs) varies from day to day. While its value is 2.5MHZ between day 23 and 24 at the equinox (September), it is 2.1MHZ at the solstice (June).

From the results obtained in error estimation, it is clearly shown that the errors associated with the mean values of foF<sub>i</sub> are less than 3 times the standard errors. The seasonal variation curve has two maximum points in the months of March and November respectively with a minimum in July. This indicates that the seasonal variation of foF<sub>2</sub> is more of a semi-annual variation.

The test of significance carried out indicates that neither seasonal variation nor Rz are responsible for the day-to-day variability in the F<sub>2</sub> region.

**Conclusion**

The results obtained in this study compared favourably with some other studies. For example Bhuyan, P.K et al (2003) indicated that the general features of the diurnal variation of F<sub>2</sub> could readily

be explained by a loss coefficient, which was substantially greater by day than at night. (Kuriyan, 1983) *J. C. Morka and D. N. Nwachukwu* to be a cause of diurnal variation. He also remarked that there is a well-marked semiannual variation in both maximum electron density and foF<sub>2</sub> of the F<sub>2</sub> region. (Adeniyi, 2004) showed that there is a seasonal variation of f<sub>0</sub>F<sub>2</sub> using Ibadan data.

One would therefore hope that the data and results established by this study be proposed as equatorial input values for the development of a variability model for the international reference ionosphere.

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